

Electric Motors and Generators

Look at a loop of wire in a magnetic field.

If you spin the wire, it induces an emf and a current - it is a generator.

$$\text{Emf} = -N\Delta\Phi/\Delta t = -NBA/t$$

If you apply an external emf, there is a current in the wires, therefore they will experience a force,

$$F_B = BIL \quad - \text{an electric motor}$$

The force causes the wire to spin. While spinning, it acts like a generator, inducing a back emf opposing the applied emf.

$$V_{\text{back}} = \text{emf} - Ir$$

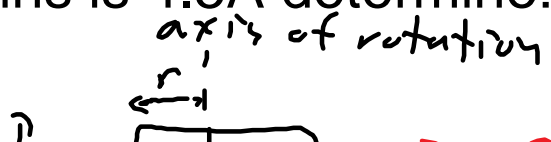
Back emf is proportional to the frequency of revolution

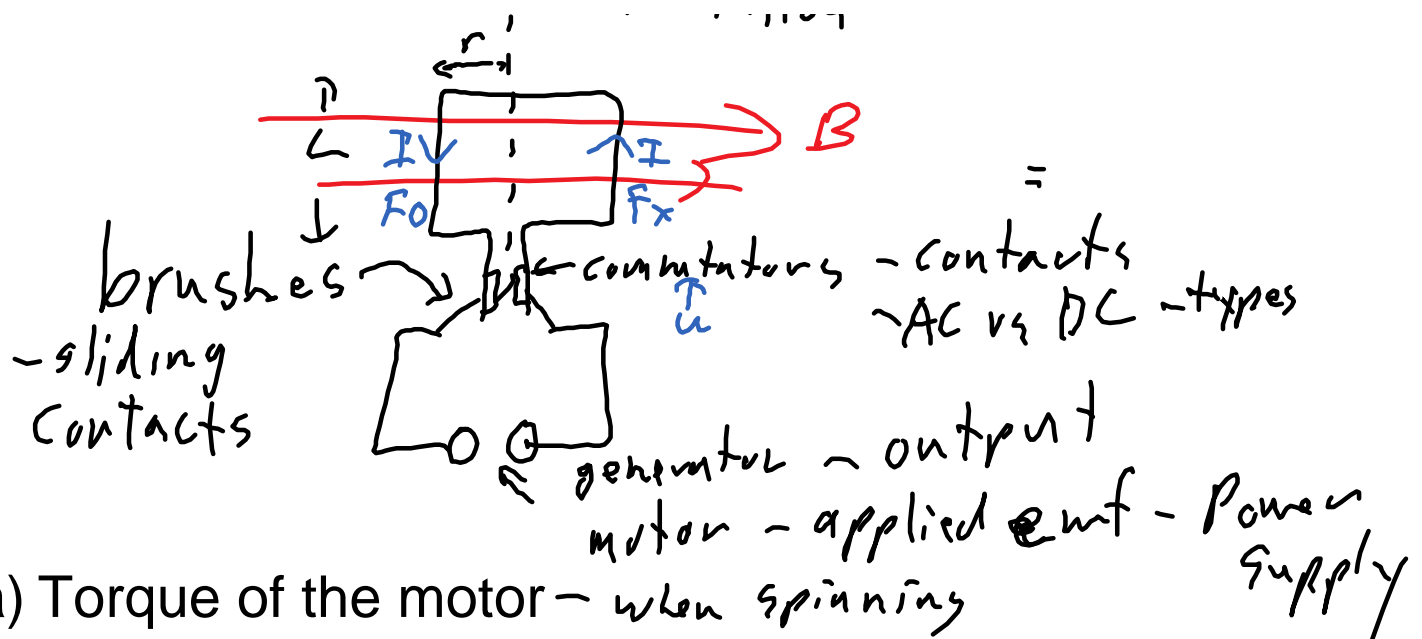
r is the resistance of the armature(wire part) of the motor

emf is the applied emf and I is the current through the motor.

Eg.

For the following motor, with 80 square loops of wire with length 1.50 cm in a 0.17T magnetic field. If the applied voltage is 6.0V and current when the armature is held is 8.5A and the current when the armature spins is 4.5A determine:





- Torque of the motor - when spinning
- Resistance of the armature
- Back emf
- Back emf if the frequency of rotation is halved.
- Bonus: The rotation frequency at full rotation.

a) $\tau = Fr$

$$\tau = 2NBILr = NBI \cancel{A} I$$

2 wire every loop

$$\tau = 80 \times 0.17 \text{ T} \times (0.015 \text{ m})^2 (4.5 \text{ A})$$

$$\tau = \boxed{0.014 \text{ Nm}}$$

0.71 Ω

b) $r = \frac{\epsilon_{mf}}{I} = \frac{6.0 \text{ V}}{8.5 \text{ A}} = \dots$

$$r = 0.014 \text{ Nm}$$

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$$0.71 \Omega$$

$$b) r = \frac{\mathcal{E}_{mf}}{I} = \frac{6.0 \text{ V}}{7.5 \text{ A}} = \dots$$

$R_{\text{not spinning}}$

$$c) V_{\text{back}} = \mathcal{E}_{mf} - Ir \quad 0.71 \Omega$$

$$= 6.0 \text{ V} - 4.5 \text{ A}$$

$$=$$

$$= 2.8 \text{ V}$$

$$d) \text{ if } f \text{ is half, } V_{\text{back}} \text{ is half} = 1.4 \text{ V}$$

$$\mathcal{E}_{mf_{\text{peak}}} = 2\pi f NBA$$

$$\mathcal{E}_{mf} \propto f$$

$$\Phi = BA \cos \theta$$

$$\theta = 2\pi f t$$